II B.Tech I Semester (R18) Regular Examinations November 2019 DISCRETE MATHEMATICS

Time : 3 hours

PART- A

(Compulsory Question 10*2=20 Marks)

- 1 a Give the symbolical representation and converse of the implication of the statement "If it is raining then I get wet".
 - b Define Predicate and explain with the help of example.
 - c Find the number of different symmetric relations that can be defined on the set $A = \{1, 2, 3, 4\}$
 - d Represent the relation $R: A \rightarrow A$, $A = \{1, 2, 3, 4, 5\}, R = \{(1, 4), (2, 3), (4, 2), (3, 3), (1, 1), (5, 1)\}$ using graph and matrix methods.
 - e If \circ is an operation on Z defined by $x \circ y = x + y + 1$, prove that (z, \circ) is an abelian group?
 - f Define the operation "under multiplication modulo 7"
 - g Show the complete graph K_5 is not a planar graph.
 - $h\$ Define the meaning of Graph coloring and $\$ chromatic number.
 - i How many different ways a 5 digit number (n) can be prepared using digits {0, 1, 2, 5, 6}, where n >5000.
 - j Define the Partition of integers with the help of example.

PART B

(Answer all the Questions Each carry 10 Marks)

- 2 a Show that $\neg P \land (\neg Q \land R) \lor (Q \land R) \lor (P \land R) \Leftrightarrow R$
 - b write the equivalence formulas of predicate statements and find the negation of the statement $\left[\forall x \exists y \left[\left(p(x, y) \land q(x, y) \right) \rightarrow r(x, y) \right] \right]$

OR

- 3 a Prove the equivalence $p \lor q \lor (\neg p \land \neg q \land r) \Leftrightarrow p \lor q \lor r$
 - b Show that $R \lor S$ follows logically from the premises $C \lor D$, $(C \lor D) \to \neg H$, $\neg H \to (A \land \neg B)$ and $(A \land \neg B) \to (R \lor S)$.
- a Let A= {1,2,3,4}.Give an example of a relation on A that is:
 i)Reflexive & Symmetric but not Transitive ii) Reflexive & Transitive, but not
 Symmetric iii) Symmetric & Transitive but not Reflexive iv)Equivalence relation
 v) Only antisymmetric
 - b. Verify the following relations are functions or not If $f: R \rightarrow R$

i)
$$f(x) = \frac{1}{x} f(x) = \frac{1}{x} x$$

ii)
$$f(x) = |x|$$

- iii) f(x) = sqrt(x)
- iv) $f(x) = \pm sqrt(x^2 + 1)$

OR

- 5 a $R: A \rightarrow A$, $A = \{1, 2, 3, 4\}, R = \{(1, 4), (2, 3), (4, 2), (3, 3), (1, 1)\}$ find the transitive closure of the relation?
 - b Define the partial order relation and compatibility relation? Give on example which is both partial and compatibility relation over a set $A = \{1, 2, 3, 4\}$

- 6 a Show that the algebraic system (A,*) is a group, where $A=\{-1,+1,-i,+i\}$ and * is a multiplication operation.
 - b Define the lattice and its properties.

OR

- 7 a Let G be a group of positive real numbers under multiplication and G' be a group of all real numbers under addition. The mapping $f: G \to G^1$ given by $f(x) = \log_{10} x$. Show that f is a Homorphism.
 - b Let G be the set of real numbers not equal to -1 and * be defined by $a*b=a+b+a\times b$. Prove that (G, *) is a group.
- 8 a Find, whether the below graphs are similar or not using procedure of graph isomorphism?



b Define Euler and Hamiltonian graphs, Find the following graph is Eularian or Hamiltonian or both?





- 9 a Define the following types of trees
 - i) Height balance tree
 - ii) Complete tree
 - iii) Fully binary tree
 - iv) Binary tree
 - b Find the optimal prefix code for the alphabets a,e,i,o,u with the frequencies 12,5,9,8,2 respectively.
- 10 a A group of 8 is composed of 5 psychologists and 3 sociologists.

a) In how many ways can a committee of 5 be formed?

b) In how many ways can a committee of 5 be formed that has 3 psychologists and 2 sociologists?

b Show that $nC_0 + nC_1 + nC_2 + \dots + nC_n = 2^n$

OR

- 11 a Find the generation function of the following sequence 0,2,612,20,30,42......
 - b. Define the rook Polynomials & Arrangement with forbidden arrangements.