

Set-12/

3 } Travelling sales-10 ~~10~~
4 }

5 } a) P class NP class (5) } Different
6 } b) NP hard, NP Complete (5)

Set-11)

1 } a) algorithm for Connected Components & spanning trees
2 } b) procedure to identify Connected components

3 } a) Control abstraction } Branch & bound
4 } b) general method }

Set-11

1 } a) in, pre, post ✓
2 } b) Compare prim's, kruskals

3 }
4 } 0/1 knapsack using branch bound ~~10~~

Set-1

1 } a) BFS
2 } b) DFS ✓

5 } a) Cook's theorem
6 } b) 3SAT problem in NP

(b) NP Complete	NP hard
* NP Complete problems are decision problem	* NP hard problem might not be decision problem
* harder problems	* hardest problems
* it is in NP	* may not be in NP
* problem x is NP Complete if NP problem y is reducible to x in polynomial time	* problem x is NP hard if NP Complete problem y is reducible to x in polynomial time
* Ex: 3SAT problem	* Ex: Halting problem

(a) P class	NP class
* if a problem can be solved in time polynomial in the size of the input it is considered an "easy" problem	* Technically "if a problem can be solved in polynomial time by a non-deterministic Turing machine, then it is in class NP"
* Class P contains problems which are solvable in polynomial time	* class NP consists of those problems that are <u>verifiable</u> in polynomial time

Set-11)

(1a)

Connected Components

Algorithm ~~Conn~~ Components (G, V)

{

for $i \leftarrow 1$ to n do

{

visited $[i] \leftarrow 0$

}

for $i \leftarrow 1$ to n do

{

if (visited $[i] = 0$) then

DFS(i);

output the newly visited
vertices with adjacent edges;

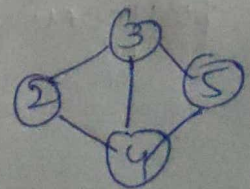
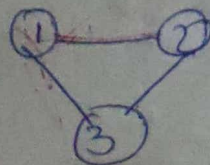
}

}

(1b)

* A undirected graph is called Connected graph if there is a path b/w any 2 vertices.

* A Connected Component is a subgraph in which any two vertices are connected to each other by paths & which is connected to no additional vertices of the super graph.



(3a)

set-1110



Control Abstraction:

Algorithm ~~branch~~ bound ()
branch

{

E ← new (node);

while (true)

{

if (E is a final ~~node~~ leaf) then

{

write ("path from E to the root");

return;

}

Expand (E);

if (H is empty) then

{

write ("there is no solⁿ");

return #;

}

E ← delete_top (H);

}

}

(3b) General method
(matter)

Set - 11

(11a)

pre order - PLR

In order - LPR

post order - LRP

Algorithm

- tree node := record

{
- type data;

- tree node * lchild;

- tree node * rchild;

}

}
Common for all

pre order

Algorithm pre order (t)

{

if (t ≠ 0) then

{

visit (t);

preorder (t → lchild);

preorder (t → rchild);

}

}

In order

Algorithm in order (t)

{

if (t ≠ 0) then

{

inorder (t → lchild);

visit (t);

inorder (t → rchild);

}

}

post order

Algorithm post order (t)

{

if (t ≠ 0) then

{

postorder (t → lchild);

postorder (t → rchild);

visit (t);

}

}

(16)

Sch-11

Prims

* it starts to build to minimum spanning tree from any vertex in the graph

* it traverses one node more than one time to get minimum distance

* Time Complexity - $O(V^2)$

* it generates the minimum spanning tree starting from the root vertex

* Applications

1. Travelling sales person
2. Network for roads and rail tracks connecting all cities

Kruskals

* it starts to build the minimum spanning tree from the vertex carrying minimum weight in the graph

* it traverses one node only once

* Time Complexity - $O(E \log V)$

* it generates the minimum spanning tree starting from the least weighted edge

* Applications

1. LAN Connection
2. TV network

Set = 1

(1a) Graph traversal
↳ BFS, DFS

BFS

Breadth first search

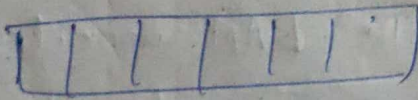
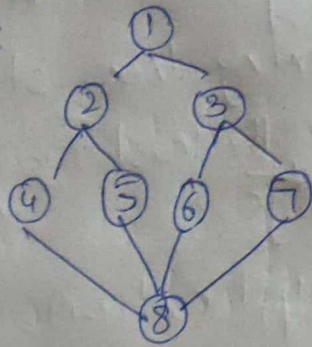
Algorithm BFS(G, n)

```

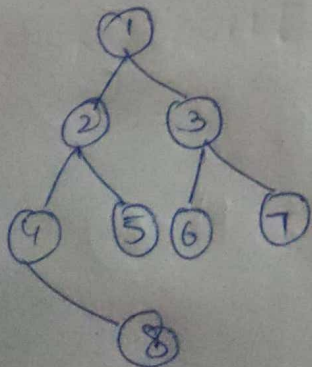
{
  for i := 1 to n do
    visited[i] := 0;
  for(i := 1 to n) do
    if (visited[i] == 0) then
      BFS(G, i);
}

```

Ex:



O/P:



1 2 3 4 5 6 7 8

(1b)

DFS

At depth first search

Algorithm DFS(G, v)

```

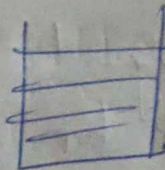
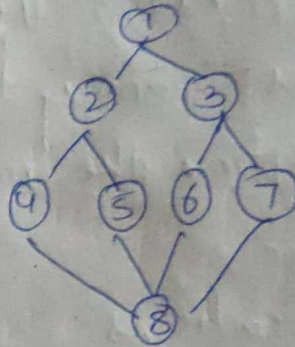
{
  v.visited := true;
  for each v ∈ G Adj[v];
  if (v.visited := false)

```

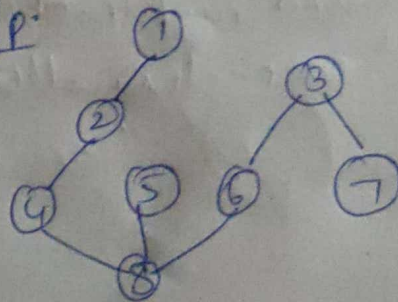
```

  DFS(G, v);
}

```



O/P:



5 7 3 6 8 4 2 1

(6a)

Cook's theorem:

Scientist Stephen Cook in 1971 stated that boolean satisfiability problem is NP-Complete

proof:

This algorithm can also determine the values of expression for corresponding assignment and can accept the entire expression is true

this algorithm is composed by

1. input type
2. read/write head
3. each cell contains only one symbol at a time
4. Computation is performed in no. of states
5. The algorithm terminates when it reaches the accept state

The conjunction clauses for boolean expressions are given in following table.

clauses	meaning	Time Complexity
$\forall ij \exists$	cell i of i/p tape contains symbol j	$O(pn^2)$
Q_{s0}	initial state	$O(1)$
H_{00}	initial position of tape head	$O(1)$
$T_{ijk} = T_{ij(k+1)} \vee H_{ik}$	tape remains unchanged unless written	$O(pn^2)$
$Q_{qk} \rightarrow \omega Q_{qk}$	one state at a time	$O(pn)$
$H_{ik} \rightarrow \omega H_{ik}$	one read/write head position at a time	$O(pn^2)$

Note: H - head
 Q - states
 T - tape

disjunction clauses for the boolean expressions

clauses	meaning	Time Complexity
$(H_{ik} \wedge Q_{jk} \wedge T_{ijk})$ \rightarrow $Q_{i(k+1)} \wedge Q_{j(k+1)} \wedge T_{ij(k+1)}$	possible transitions	$O(pcn^2)$
disjunction of all clauses \wedge	moving to accept state	$O(1)$

if B is satisfiable then there is an accepting state in the algorithm. This the proof shows that boolean satisfiability problem solved in polynomial time. Hence all problem in NP could be solved in polynomial time and hence class NP could be equal to P.

Note: H - head

Q - states

T - tape

disjunction clauses for the boolean expressions

clauses	meaning	Time Complexity
$(H_{ik} \wedge Q_{jk} \wedge T_{ijk})$ \rightarrow $(H_{(i+j)(k+1)} \wedge Q_{j(k+1)} \wedge T_{ij(k+1)})$	possible transitions	$O(pcn^2)$
disjunction of all clauses $\wedge Q$	moving to accept state	$O(1)$

if B is satisfiable then there is an accepting state in the algorithm. This the proof shows that boolean satisfiability problem solved in polynomial time. Hence all problem in NP could be solved in polynomial time and hence class NP could be equal to P.

set - II

(6b)

3SAT problem

3SAT problem which takes a boolean formula 'S' in CNF form with each clause having exactly three literals and check whether S is satisfied or not
~~for~~ formula for instance of 3SAT problem

$$S = (\bar{a} + b + \bar{g}) \cdot (c + \bar{e} + f) \cdot (\bar{b} + d + \bar{f}) \cdot (a + e + b)$$

Theorem: 3SAT problem in NP

proof: let 'S' be the boolean formula having 3 literals in each clause for which we can construct a simple non-deterministic algorithm which can guess an assignment if boolean values to 'S' is evaluated as 1 then 'S' is satisfied and we can say that 3SAT is NP Complete.